

# Electric-field-induced strain for $(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3$ -based lead-free multilayer actuator

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Multilayer prototype actuators were demonstrated using  $(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3$  [BNT]-based ceramics as active layers and Pt as internal electrodes. One of the BNT-based solid solutions,  $0.68(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3-0.04(\text{Bi}_{1/2}\text{Li}_{1/2})\text{TiO}_3-0.28(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3$  (BNLKT4–28) has been selected as the active layer and it showed a relatively large piezoelectric strain constant  $d_{33}$  of 130 pC/N and a high depolarization temperature  $T_d$  of 226°C. The total number of layers was 10 and the active layer thickness was 125  $\mu\text{m}$  for the sintered body. The final compact dimensions were approximately  $5 \times 5 \times 2 \text{ mm}^3$ . From the SEM observation, there were no apparent delaminations around the interface between Pt electrodes and active BNLKT layers. The large electric-field-induced strain at 70 kV/cm was 0.17% and the longitudinal dynamic displacement at the same electric field was 2.1  $\mu\text{m}$ .

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## 1. Introduction

Piezoelectric materials play an important role in electrical devices, such as actuators, accelerators, piezoelectric motors, transducers, filters, and resonators. Most piezoelectric devices are composed of  $\text{Pb}(\text{Zr,Ti})\text{O}_3$  (PZT)-based piezoelectric ceramics because of their excellent piezoelectric properties.<sup>1),2)</sup> However, PZT ceramics contain a large amount of PbO; therefore, lead-free piezoelectric materials used to replace PZT have recently been required from the viewpoint of environmental protection. In particular, actuator applications have a large market in piezoelectric devices; thus, the development of lead-free piezoelectric materials is strongly demanded in the actuator field. As the lead-free piezoelectric candidates for actuators, various perovskite-structured ferroelectrics, such as  $\text{BaTiO}_3$  (BT),  $(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3$  (BKT),  $(\text{K,Na})\text{NbO}_3$  (KNN), and  $(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3$  (BNT)-based solid solutions, have recently been actively studied.<sup>3)–23)</sup> In particular, KNN-based ceramics, such as textured LF4,<sup>6)</sup> are expected to be the best material for lead-free actuators owing to their excellent piezoelectric strain constant  $d_{33}$  of  $\sim 400 \text{ pC/N}$ . Moreover, KNN-based multilayer piezoelectric ceramics with nickel inner electrodes have been developed, and they exhibited a large electric-field-induced strain.<sup>24)</sup> On the other hand, raw materials, such as  $\text{Nb}_2\text{O}_5$  and  $\text{K}_2\text{CO}_3$ , are very expensive compared with PZT-based materials, and their processing cost is also high owing to the difficulties and complications in their manufacturing process. Therefore, the economical issue may be a stumbling block in the progress of the practical application of KNN based materials in actuators.

BNT ceramics are expected to be one of the superior candidates for lead-free piezoelectric materials owing to their friendly for current manufacturing process, low material cost, and relatively high piezoelectric properties.<sup>13)–23)</sup> However, these ceramics exhibit a high coercive field ( $E_c = 73 \text{ kV/cm}$ ), resulting

in problems in the poling process. Therefore, BNT has been modified using many materials, such as  $\text{BaTiO}_3$  (BT),<sup>3),15)</sup>  $\text{KNbO}_3$  (KN),<sup>33)</sup>  $(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3$  (BKT),<sup>16),25),26)</sup> All of these solid solutions show improved piezoelectric properties and easy treatment of the poling process by such modification as compared with pure BNT ceramics. However, the  $d_{33}$  values of these materials are still not as large as these of PZT- and KNN-based materials. To cover the low  $d_{33}$  values of BNT-based materials, it is generally considered that a multilayer structure is very effective for actuator applications because the total displacement can be increased proportionally to the layer number of the multilayer structure. However, there have been no reports on the multilayer structure of BNT-based ceramics. In this study, a prototype of the multilayer structure was prepared using BNT-based materials and Pt inner electrodes.

Selecting the BNT-based composition, we took into account the working temperature range. The crystal structure of BNT is rhombohedral at RT, and the rhombohedral-tetragonal phase transition temperature  $T_{R-T}$  and the Curie temperature  $T_C$  are approximately 300 and 540°C on heating, respectively, for a BNT single crystal.<sup>27)–29)</sup> In addition, BNT has a depolarization temperature  $T_d$  of approximately 185°C. Although it has been reported that  $T_d$  is the phase transition temperature between ferroelectric and antiferroelectric phases,<sup>30)</sup> the nature of the phase transition is not yet clear. Moreover, the working temperature is limited by  $T_d$ ; thus, is very important for practical applications. Recently, we have reported that  $x(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3-y(\text{Bi}_{1/2}\text{Li}_{1/2})\text{TiO}_3-z(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3$ , [BNLKT100] $y$ -100 $z$  ( $x+y+z=1$ ) solid solution shows relatively high  $T_d$  values of higher than 200°C and a relatively large  $d_{33}$  of 150 pC/N.<sup>31),32)</sup> Note again that the displacement can be enlarged by increasing the layer number of the multilayer structure; however  $T_d$  is a material characteristic that is difficult to control extrinsically. In this study, multilayer piezoelectric ceramics were demonstrated using the BNLKT4–28 composition for the active piezoelectric layer to see the stability of multilayer structure, phase transition temperature and strain behavior.

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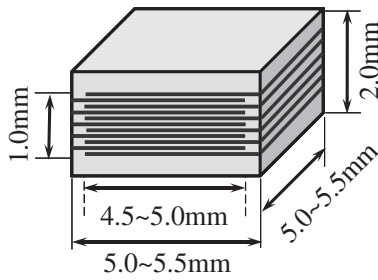


Fig. 1. Schematic diagram of green compact.

## 2. Experimental procedure

BNKLT ceramics were prepared by a conventional ceramic fabrication technique. Reagent-grade metal oxide or carbonate powders of  $\text{Bi}_2\text{O}_3$ ,  $\text{TiO}_2$ ,  $\text{Na}_2\text{CO}_3$ ,  $\text{K}_2\text{CO}_3$ , and  $\text{Li}_2\text{CO}_3$  were used as starting materials. Starting raw materials were mixed in ethanol with stabilized zirconia balls by ball milling for 24 h. After drying, the mixed powders were calcined at  $800^\circ\text{C}$  for 4 h. The calcined powders were ground again by ball milling for 6 h. The particle sizes of the milled powders were controlled to be  $1\text{--}2\ \mu\text{m}$ . The slurries for tape casting were prepared by mixing the calcined powders, solvent, binder and plasticizer. As inner electrodes, platinum paste (ML-3822, Shoen Chemical Inc.) was screen-printed on the sheet. Each sheet was laminated and cut to form the green compact shown in **Fig. 1**. The final dimensions of the green compact were about  $5.5 \times 5.5 \times 2.0\ \text{mm}^3$ . The total number of layers was 10 and the active layer thickness was about  $100\ \mu\text{m}$  for the sintered body. The green compact was heated to remove organic components and then sintered at  $1120^\circ\text{C}$  for 2 h. The calcined and ball-milled powders were also pressed into bulk pellets, and the pellets were sintered at  $1120^\circ\text{C}$  for 2 h in air for comparison with multilayer samples.

The crystal structures and lattice constants of the sintered bulk ceramics were confirmed by X-ray powder diffraction analysis using an X-ray diffractometer (Rigaku; RINT2000,  $\text{Cu K}\alpha$ ). Microstructures were observed by scanning electron microscopy (SEM, Hitachi S-2400). Fired-on silver was used as electrodes connected to each inner electrode for the measurement of electrical properties. Resistivities were measured using a high resistance meter (YHP 4339B). The temperature dependences of the dielectric properties were measured using an automated dielectric measurement system with a multifrequency LCR meter (YHP 4275A and Wayne Kerr 6440B) at  $1\text{ k--}1\ \text{MHz}$ . Electric-field-induced strains were measured with unipolar driving at  $0.1\ \text{Hz}$  using a contact-type displacement sensor (Millitron Model 1240). The normalized  $d_{33}^*$  is defined as follows.

$$d_{33}^* [\text{pm/V}] = \frac{S [\%]}{E [\text{kV/cm}]} \times 10^5 \quad (1)$$

The bulk specimens for the measurement of piezoelectric properties were poled in a silicone oil bath at RT by applying a  $5\ \text{kV/mm}$  DC electric field for 5 min. After poling,  $k_{33}$  was determined by a resonance-antiresonance method using an impedance analyzer (Agilent 4294A). The free permittivity  $\epsilon_{33}^T$  was determined from the capacitance at  $1\ \text{kHz}$  of the poled specimen. The elastic constants  $s_{33}^E$  were calculated from the frequency constant  $N_{33}$  and the measured density,  $\rho_0$ . Finally, the piezoelectric constants  $d_{33}$  were calculated from  $k_{33}$ ,  $\epsilon_{33}^T$  and  $s_{33}^E$  using,

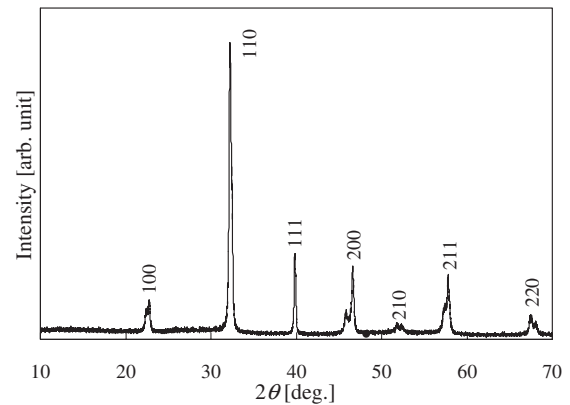
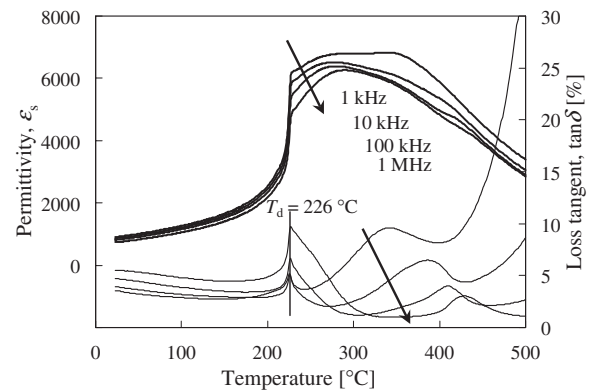


Fig. 2. X-ray diffraction pattern for BNLKT4-28.

Fig. 3. Temperature dependences of dielectric constant  $\epsilon_s$  and loss tangent  $\tan \delta$  for poled BNLKT4-28.

$$d_{33} = k_{33} \sqrt{\epsilon_{33}^T \cdot s_{33}^E} \quad (2)$$

## 3. Results and discussion

### 3.1 Bulk characteristics of BNLKT4-28 ceramics

**Figure 2** shows an X-ray diffraction (XRD) pattern for a BNLKT4-28 ceramic showing a single phase of a perovskite structure with tetragonal symmetry. The lattice constants calculated from the XRD pattern were  $a = 3.895$  and  $c = 3.928\ \text{\AA}$ , and the lattice anisotropy (tetragonality)  $c/a$  was 1.0085. This anisotropy is relatively large and approximately the same as that in  $\text{BaTiO}_3$ . The relative density of the bulk sample sintered at  $1120^\circ\text{C}$  for 2 h is higher than 96%. The volume resistivity  $\rho$  of bulk BNLKT4-28 is about  $5 \times 10^{12}\ \Omega\cdot\text{cm}$ . **Figure 3** shows the temperature dependences of the dielectric properties  $\epsilon_s$  and loss tangent  $\tan \delta$  of bulk BNLKT4-28. The depolarization temperature,  $T_d$ , was determined to be  $226^\circ\text{C}$  from the peaks of  $\tan \delta$ . This temperature is consistent with that determined from the temperature dependences of piezoelectric properties. **Figure 4** shows the frequency dependence of the impedance  $Z$  of the (33) mode for BNLKT4-28. The electromechanical coupling factor  $k_{33}$  is 0.45, and the calculated piezoelectric strain constant  $d_{33}$  is  $130\ \text{pC/N}$ . From the measurement of the electric-field-induced strain  $S$  for the bulk sample, the normalized  $d_{33}^*$  value was calculated to be  $218\ \text{pm/V}$  at  $80\ \text{kV/cm}$  using formula (1). The  $d_{33}^*$  value is about 1.6-fold as large as the  $d_{33}$  value determined from the resonance and antiresonance method. Generally, the electric-field-induced strain consists of intrinsic and extrinsic effects. The intrinsic effect is due to the deformation of the

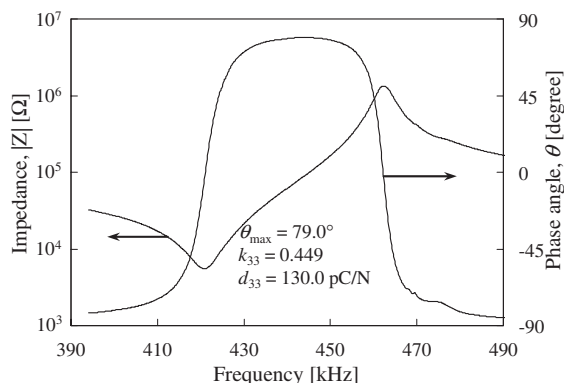


Fig. 4. Frequency dependence of impedance  $Z$  for bulk BNLKT4-28 in (33) mode.

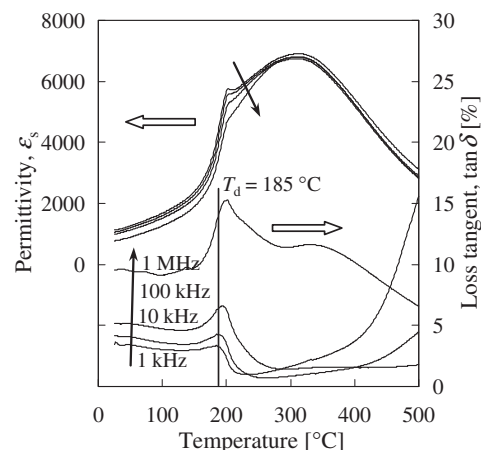


Fig. 6. Temperature dependences of dielectric constant  $\epsilon_s$  and loss tangent  $\tan \delta$  for multilayered BNLKT4-28.

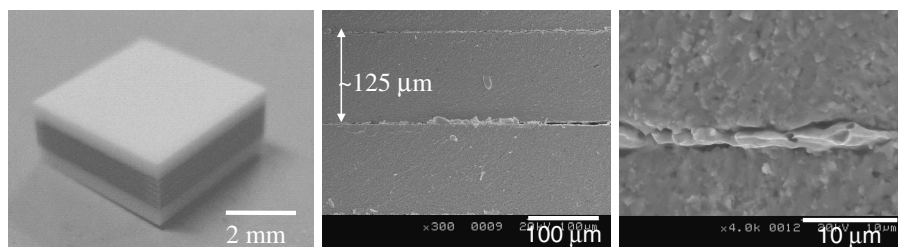


Fig. 5. Images of (a) external view and (b), (c) SEM micrographs.

crystal lattices by the electric-field. The  $d_{33}$  values obtained by the resonance technique correspond to the intrinsic effect. On the other hand, the differences between  $d_{33}^*$  and  $d_{33}$  are associated with the extrinsic effects. Masuda analyzed the electric-field-induced strain of modified PZT as a superimposition of piezoestriction (intrinsic effect) and electrostriction (extrinsic effect), where the electrostriction was mainly caused by the domain contribution.<sup>34)</sup> Also, Tsurumi confirmed experimentally, by in situ XRD analysis, that the electric-field-induced strains of tetragonal PZT ceramics were composed of strain due to the intrinsic piezoelectric and extrinsic effects from  $90^\circ$  domain-wall motions.<sup>35),36)</sup> The electric-field-induced phase transformation is also involved in the extrinsic effect, but BNLKT4-28 has no phase transition at room temperature.<sup>31),32)</sup> Therefore, in the case of BNLKT4-28 ceramics with tetragonal symmetry, the origins of these differences between  $d_{33}^*$  and  $d_{33}$  seem to be the  $90^\circ$  domain-wall motions.

### 3.2 Multilayer characteristics

**Figure 5** shows the images of (a) the external view and (b), (c) SEM micrographs after the co-firing of multilayered BNLKT4-28 at  $1120^\circ\text{C}$  for 2 h. We could not observe the apparent bending of the sample in the external view. From SEM micrograph (b), the active layer thickness between electrodes was estimated to be approximately  $125\ \mu\text{m}$  for the sintered body. The average active layer thickness was calculated from some layer thicknesses in the SEM images to be  $124.4\ \mu\text{m}$ , and is used for the calculation of the dielectric constant  $\epsilon_r$  and resistivity  $\rho$  of the multilayered samples. SEM micrograph (c) indicates a homogeneous microstructure of active BNLKT layers with grain sizes of  $1\text{--}2\ \mu\text{m}$ . In SEM micrograph (c), the interface between BNLKT and the Pt electrode is clearly distinguished and there are no significant signs of reaction or diffusion between them. On the other hand,

the adhesion between them appears relatively weak, but there are no measured data about this at present.

The  $\rho$  values of all co-fired samples are about  $10^{10}\ \Omega\cdot\text{cm}$  on average. This value is 2 orders of magnitude lower than that of bulk ceramics. Anyhow, the  $\rho$  value of  $10^{10}\ \Omega\cdot\text{cm}$  is sufficiently to apply a high DC electric field to the sample for  $S$ - $E$  measurement. **Figure 6** shows the temperature dependences of the dielectric constant  $\epsilon_r$  and loss tangent,  $\tan \delta$  for the multilayer sample. The  $\epsilon_r$  of the multilayer sample at RT is almost the same as that of the bulk ceramic. However, the  $T_d$  of  $185^\circ\text{C}$  for the multilayered sample is lower than that of the bulk ceramic. Some possible reasons for the  $T_d$  difference between the bulk and multilayered samples can be considered; one is the induced stress in the multilayer structure and another is the compositional variation. For example, in the case of  $\text{BaTiO}_3$  (BT) thin films, Yanase et al. reported that the Curie temperature  $T_C$  was increased by the large lattice misfit strain in the heteroepitaxial BT films on  $\text{SrRuO}_3$ .<sup>37)</sup> Therefore, it is considered that the phase transition temperature can be changed by an induced stress. On the other hand, Nakano et al., revealed the residual stress in BT-based multilayer ceramic capacitors (MLCCs) and the temperature dependences of their dielectric properties, indicating the absence of a significant shift in  $T_C$  with increasing residual stress up to about 200 MPa.<sup>38),39)</sup> From those reports, it is considered that the effect of an induced stress has a small contribution to the  $T_d$  difference between the bulk and multilayered samples; however, it has not yet been clarified in the case of BNT-based ceramics so far. By considering the second possible reason (i.e. compositional variation),  $T_d$  was observed to markedly decrease with decreasing  $(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3$  content in the BNLKT system.<sup>31),32)</sup> Therefore, it is speculated that the evaporation of Bi and K ions during baking and firing strongly affects the decrease in  $T_d$  in the multilayered samples. The reduction in resistivity in

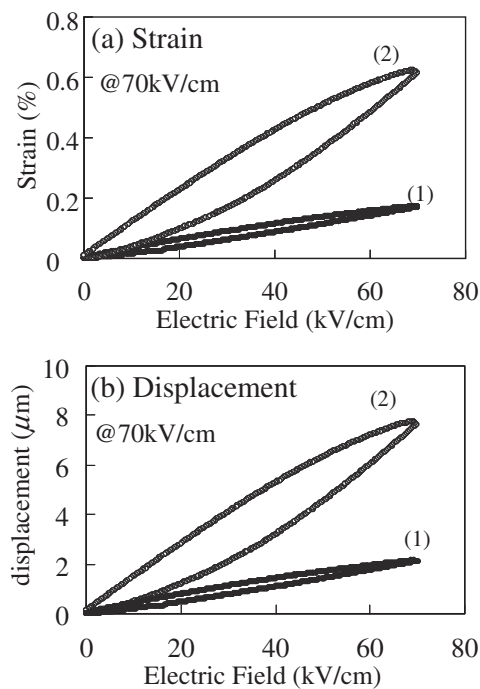


Fig. 7. (a) Electric-field-induced strain  $S$  and (b) displacement under unipolar driving at 70 kV/cm, (1) before and (2) after applying 80 kV/cm.

the multilayered samples seems to support the idea of the evaporation of Bi and K ions.

**Figure 7(a)-(1)** shows the electric-field-induced strain  $S$  under unipolar driving at 70 kV/cm. A large electric-field-induced strain of 0.17% at 70 kV/cm was obtained before applying 80 kV/cm, and the longitudinal dynamic displacement at the same electric field shown in Fig. 7(b)-(1) was 2.1  $\mu\text{m}$ . The normalized  $d_{33}^*$  was calculated to be 248 pm/V, which is similar to that in the bulk samples. This result indicates that our BNT-based multilayered prototype efficiently functioned under the unipolar driving up to 70 kV/cm. However, upon the application of a the high electric field of 80 kV/cm, both strain and displacement reached the extremely high values of 0.62% and 7.74  $\mu\text{m}$ , respectively, at 70 kV/cm. The  $d_{33}^*$  at that time was about 850 pm/V, which was extraordinarily large, as we expected. To understand this behavior, the  $S$ - $E$  curve was measured using a single-layer specimen prepared from a multilayer sample. The single-layer specimen of 125  $\mu\text{m}$  thickness also indicated a large  $d_{33}^*$  of about 3000 pm/V at 80 kV/cm. This is obviously due not to the longitudinal piezoelectric and electrostrictive effects but to the bending effect. From this result, it is speculated that the large  $d_{33}^*$  ( $\sim 850$  pm/V) in the 10-layer specimen is also suspected due to the bending effect after applying 80 kV/cm. In other words, certain interfaces between Pt electrodes and piezoelectric active layers were delaminated by an induced high electric field at 80 kV/cm, and then, the piezoelectric active layers were partially bend similarly to a Moonie structure<sup>40),41)</sup> and a tailor-made multilayer piezoelectric actuator.<sup>42),43)</sup>

#### 4. Summary

A lead-free multilayer actuator was demonstrated using a bismuth sodium titanate,  $(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3$  [BNT], -based solid solution  $[x(\text{Bi}_{1/2}\text{Na}_{1/2})\text{TiO}_3-y(\text{Bi}_{1/2}\text{Li}_{1/2})\text{TiO}_3-z(\text{Bi}_{1/2}\text{K}_{1/2})\text{TiO}_3,$

(BNLKT100y-100z, BNLKT4-28)] and Pt internal electrodes in this study. The bulk BNLKT4-28 shows a relatively large piezoelectric strain constant  $d_{33}$  of 130 pC/N and high depolarization temperature  $T_d$  of 226°C. In the prototype multilayer structure, the total number of layers was 10 and the active layer thickness was 125  $\mu\text{m}$  for the sintered body. The final compact dimensions were approximately  $5 \times 5 \times 2 \text{ mm}^3$ . From the SEM observation, we could not observe any apparent delamination around the interface between Pt electrodes and active BNLKT layers. The large electric-field-induced strain  $S$  at 70 kV/cm was 0.17% and the longitudinal dynamic displacement at the same electric field was 2.1  $\mu\text{m}$ . Our demonstration of a BNT-based multilayered prototype was successful and showed a large displacement under unipolar driving up to 70 kV/cm.

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